

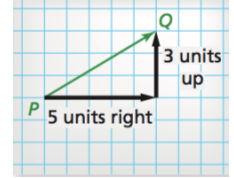
# Chapter 4 Transformations

## Ch 4.1 Translations

### Vocabulary

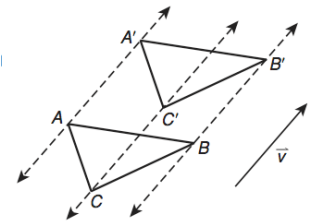
Transformation: \_\_\_\_\_

Vector: \_\_\_\_\_

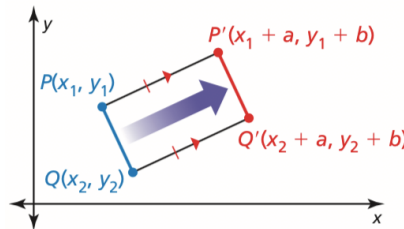


Translation: \_\_\_\_\_

Isometry: \_\_\_\_\_

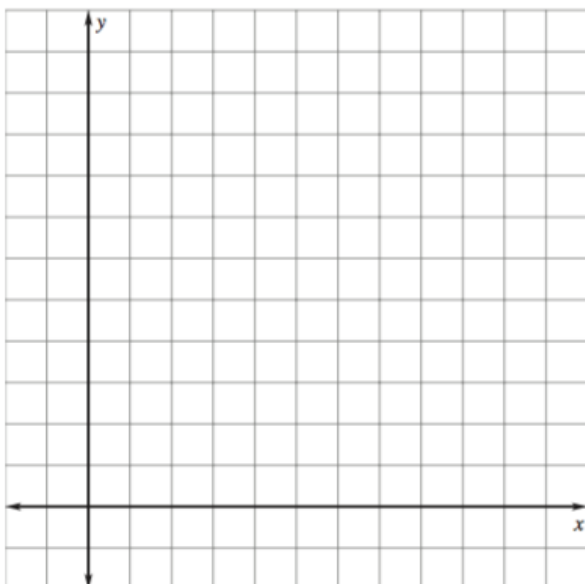


### Definition of Translation:



### Graph:

The vertices of  $\triangle ABC$  are  $A(0, 3)$ ,  $B(2, 4)$ , and  $C(1, 0)$ . Translate  $\triangle ABC$  using vector  $\langle 5, -1 \rangle$ .



### Translation Vector

#### Component Form

$$\langle 4, 3 \rangle$$

$$\langle -3.2, 5.9 \rangle$$

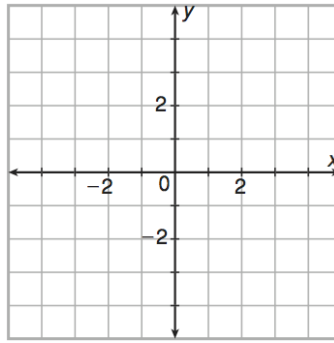
$$\langle t - 1, 2t^2 \rangle$$

#### Translation Rule

**Graph:**

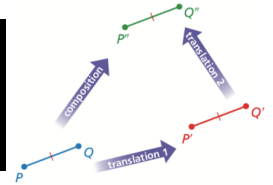
Pre-image: A(1, -2), B(1, 0), C(3, 1), D(4, -3)

Rule:  $(x, y) \rightarrow (x-5, y+3)$

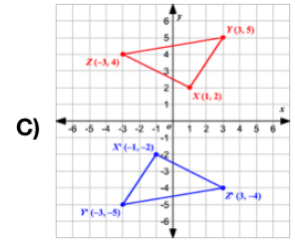
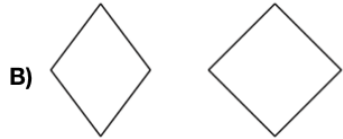
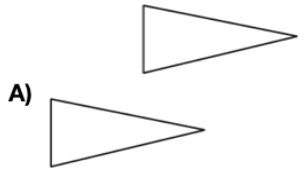


Composition of Transformations: \_\_\_\_\_

<b>Composition Theorem</b>	
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**Is this a translation? Why or why not?**



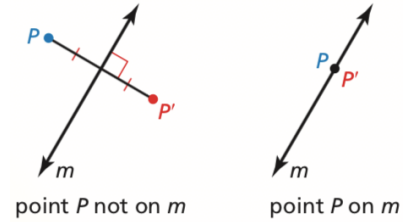
## Ch 4.2 Reflections

### Vocabulary

Reflection: \_\_\_\_\_

Line of Reflection: \_\_\_\_\_

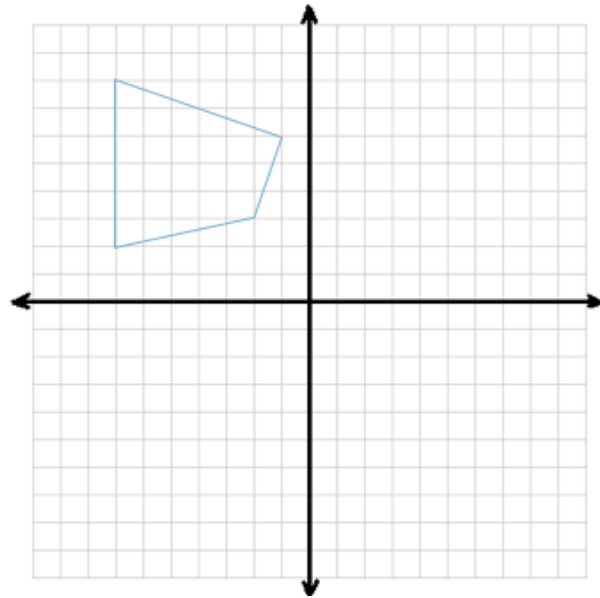
#### Definition of Reflection:



#### Graph:

Reflect the pre-image about the:

- a) x-axis
- b) y-axis

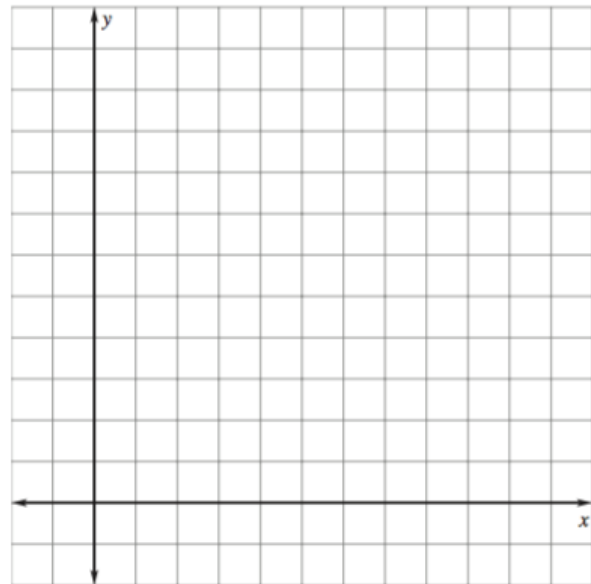


#### Graph:

Pre-image:  $A(1, 3)$ ,  $B(5, 2)$ ,  $C(2, 1)$

Reflect about the line:

- (a)  $x = 5$
- (b)  $y = 4$

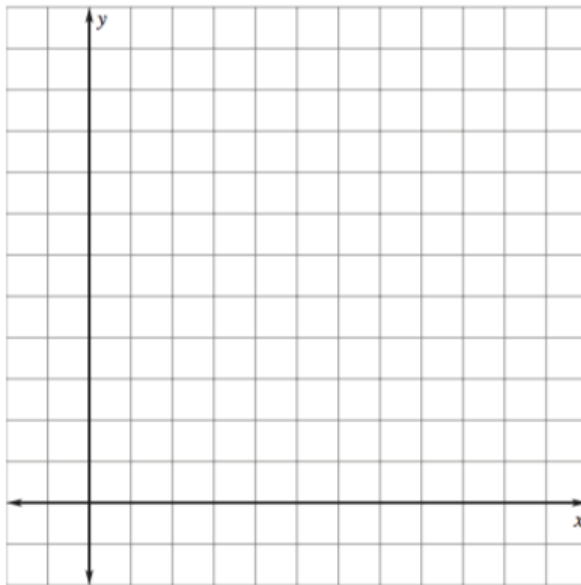


#### Challenge:

make a rule for (a)

**Graph:**

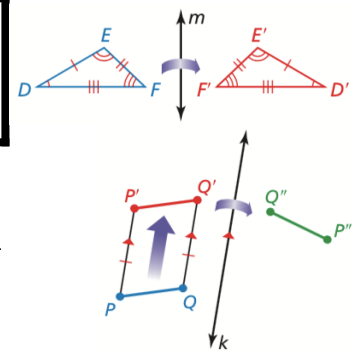
Pre-image: A(1, 3), B(5, 2), C(2, 1)  
 Reflect about the line:  $y = x$



**Rules of Reflection**

Line of Reflection	Rule
across the x-axis	
across the y-axis	
across the line $y = x$	
across the line $y = -x$	

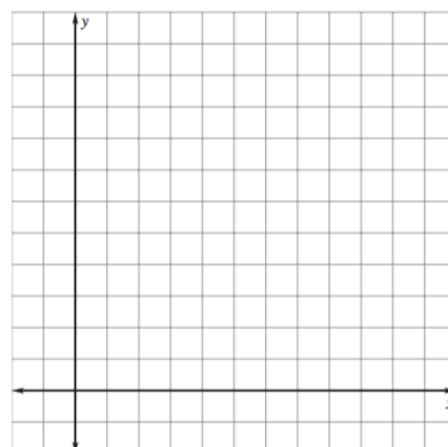
<b>Reflection Postulate</b>	
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Glide Reflection: \_\_\_\_\_

**Graph:**

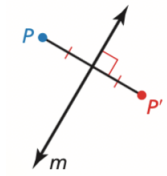
Pre-image: A(1, 3), B(5, 2), C(2, 1)  
 Perform a glide reflection using:  
 Translation  $(x, y) \rightarrow (x+5, y-1)$   
 Reflect around  $x = 3$



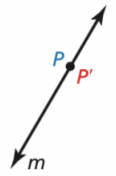
### Vocabulary

Line Symmetry: \_\_\_\_\_

Line of Symmetry: \_\_\_\_\_

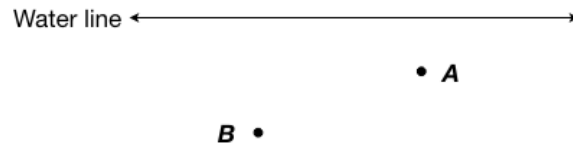


point  $P$  not on  $m$



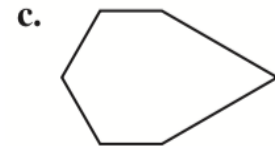
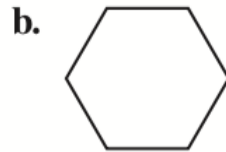
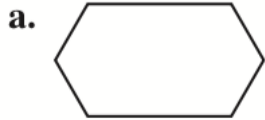
point  $P$  on  $m$

### Problem Solving - Water line



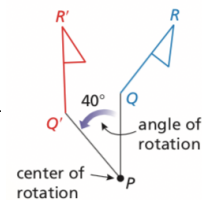
### Lines of Symmetry

How many lines of symmetry does each figure have?



## Ch 4.3 Rotations

Rotation: \_\_\_\_\_



**Definition of Rotation:**

Is this a rotation?

**A)**



**B)**



**C)**



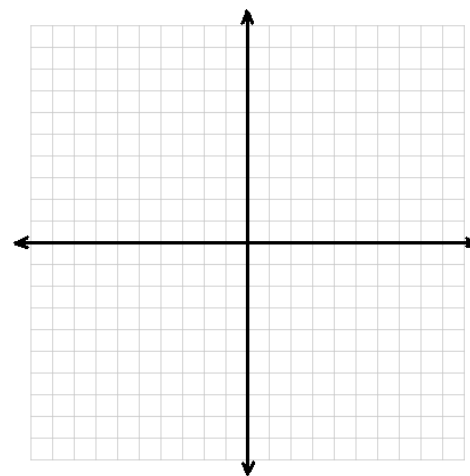
### Rules of Rotation

Rotation about the origin	Rule
rotation of $90^\circ$	
rotation of $180^\circ$	
rotation of $270^\circ$	

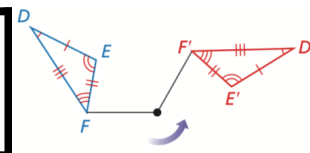
### Graph:

Pre-image:  $R(3, 1)$ ,  $S(5, 1)$ ,  $T(5, -3)$ ,  $U(2, -1)$

Graph the image rotated  $270^\circ$  about the origin.



**Rotation Postulate**

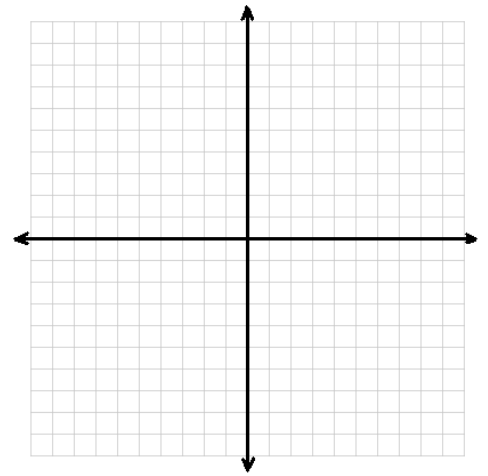


**Graph composite:**

segment R(1, -3), S(2, -6)

Reflection: around the y-axis

Rotation: 90° about the origin



**Vocabulary**

Rotational Symmetry: \_\_\_\_\_

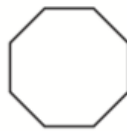
Center of Symmetry: \_\_\_\_\_

Does each figure have rotational symmetry?

a. parallelogram



b. regular octagon



c. trapezoid



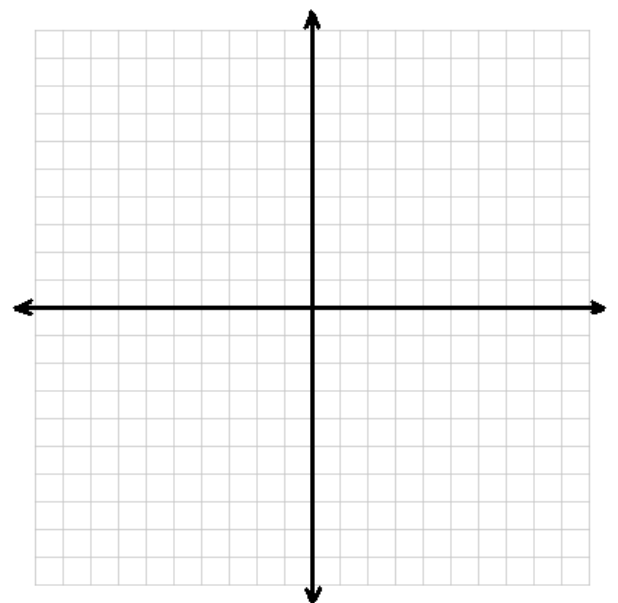
**Application - London Eye**

Observation wheel radius = \_\_\_\_\_

One rotation takes \_\_\_\_\_ minutes

If car starts at \_\_\_\_\_, what is car's location after

\_\_\_\_\_ minutes?



## Ch 4.4 Congruence and Transformations

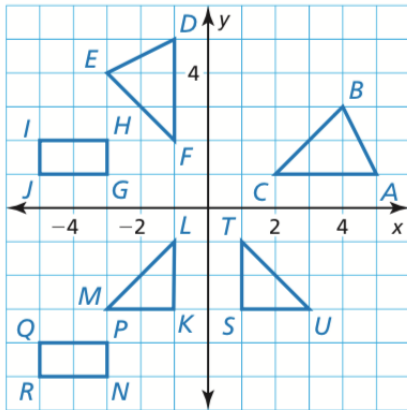
### Vocabulary

Congruent Figures: \_\_\_\_\_

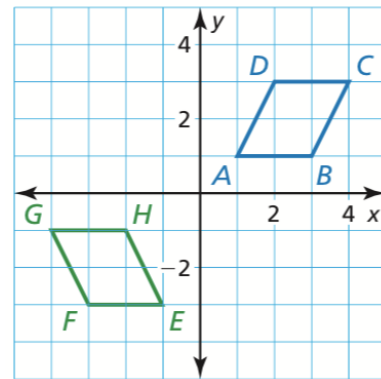
Congruence Transformation: \_\_\_\_\_

### Solve:

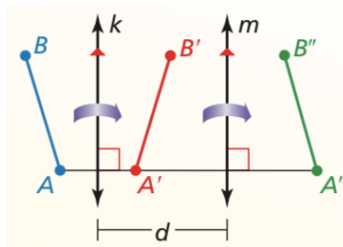
Identify congruent figures in the diagram, and determine the rigid motions (isometries) that were used.



Describe a congruence transformation that maps  $\square ABCD$  to  $\square EFGH$ .



### Reflections in Parallel Lines Theorem



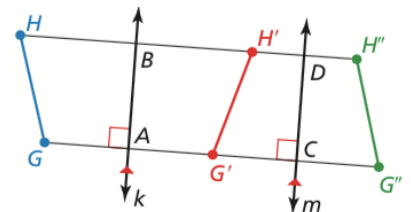
### Solve:

In the diagram, a reflection in line  $k$  maps  $GH$  to  $G'H'$ . A reflection in line  $m$  maps  $G'H'$  to  $G''H''$ . Also,  $HB = 9$  and  $DH'' = 4$ .

a. Name any segments congruent to:  $GH$ ,  $HB$ , and  $GA$ .

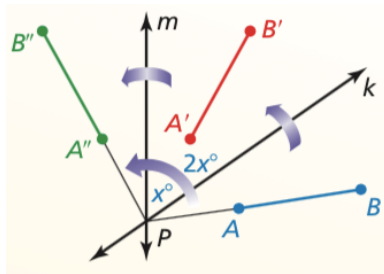
b. Does  $AC = BD$ ?

c. What is the length of  $GG''$ ?



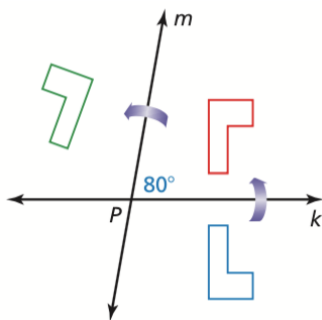


**Reflections in Intersecting Lines Theorem**



**Solve:**

In the diagram, the pre-image is reflected in line k, then in line m. Describe a single transformation that maps the blue figure onto the green figure.



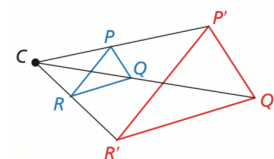
**Ch 4.5 Dilations**

**Vocabulary**

Dilation: \_\_\_\_\_

Dilation is/is not a rigid motion. Why?

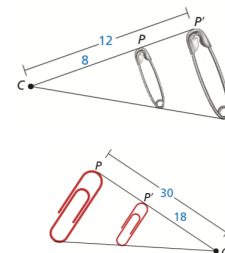
**Definition of Dilation:**



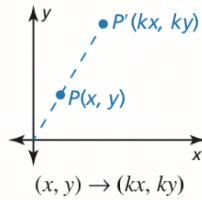
**Scale Factor:**

When scale factor \_\_\_\_\_, the dilation is an \_\_\_\_\_.

When scale factor \_\_\_\_\_, the dilation is a \_\_\_\_\_.



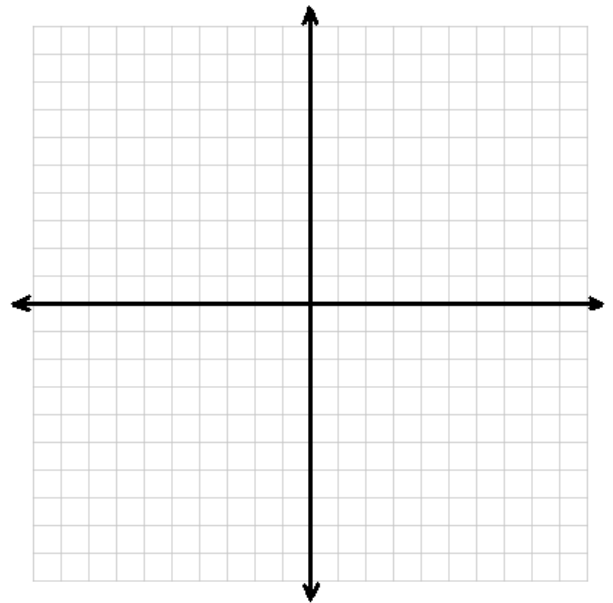
**Rule of Dilation:**



**Graph the dilation:**

Pre-image is K(-3, 6), L(0, 6), M(3, 3), and N(-3, -3).

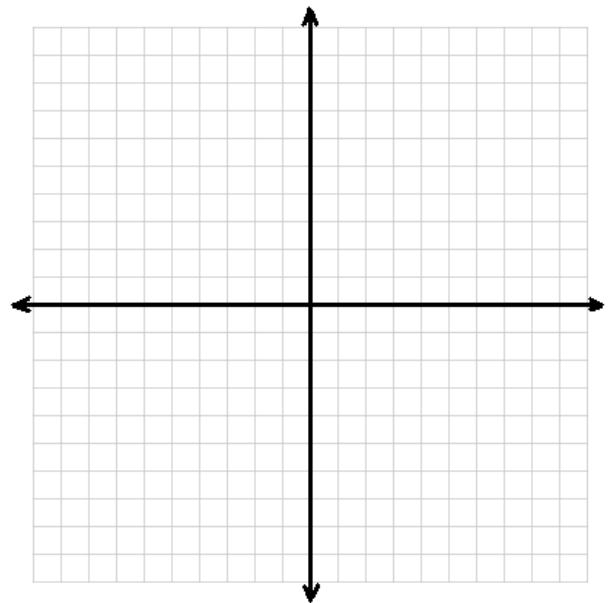
Scale factor  $k = \frac{1}{3}$



**Graph the dilation:**

Pre-image is F(-4, -2), G(-2, 4), and H(-2, -2)

Scale factor  $k = -\frac{1}{2}$



**Problem solving:**

You are using a magnifying glass that shows the image of an object that is \_\_\_\_\_ times the object's actual size. Determine the length of the image of the spider seen through the magnifying glass.



## Ch 4.6 Similarity and Transformations

### Vocabulary

Similar Geometries: \_\_\_\_\_

Similarity Transformation: \_\_\_\_\_

### Definition of Similar Figures:

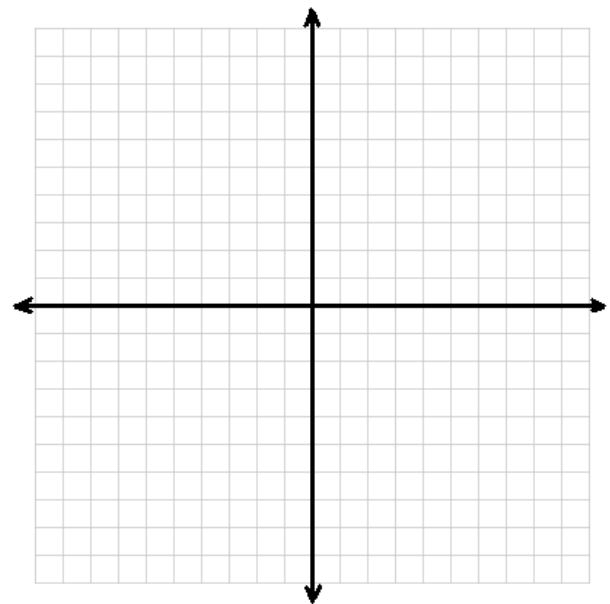


### Perform a Similarity Transformation

Graph  $\triangle ABC$  with vertices  $A(-4, 1)$ ,  $B(-2, 2)$ , and  $C(-2, 1)$  and its image after the similarity transformation.

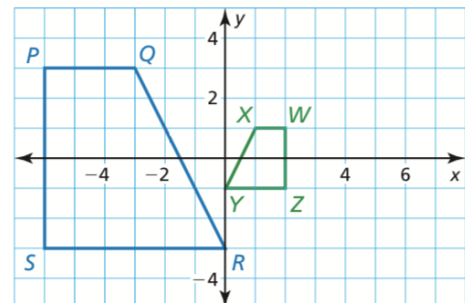
Translation:  $(x, y) \rightarrow (x + 5, y + 1)$

Dilation:  $(x, y) \rightarrow (2x, 2y)$



### Describe a Similarity Transformation

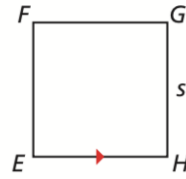
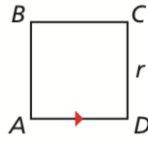
Describe transformation(s) that maps trapezoid PQRS to trapezoid WXYZ.



### Prove two squares are similar

**Given** Square  $ABCD$  with side length  $r$ ,  
square  $EFGH$  with side length  $s$ ,  
 $\overline{AD} \parallel \overline{EH}$

**Prove** Square  $ABCD$  is similar to  
square  $EFGH$ .



Statements

Reasons